

Optimal Feature Extraction and Feature Subsets for Various Machine Learning Algorithms Targeting Freezing of Gait Detection

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Okinawa Institute of Science and Technology Okinawa, Japan

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- 1. Background
- 2. FEATURE EXTRACTION
- 3. FEATURE SELECTION
- 4. CONCLUSION



Freezing of Gait Research Objective Research Challenges Purpose of This Work

BACKGROUND

Freezing of gait and the research behind it.

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FREEZING OF GAIT RESEARCH OBJECTIVE RESEARCH CHALLENGES PURPOSE OF THIS WORK

Freezing of Gait

▶ Irregular gait pattern associated with Parkinson's disease

An episodic inability lasting seconds to generate effective stepping



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Freezing of Gait

▶ Irregular gait pattern associated with Parkinson's disease

An episodic inability lasting seconds to generate effective stepping

- Roughly 50% prevalence among PD patients
- Mostly observed during turns, gait initiation, passing narrow spaces, stressful situations, reaching destination

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FREEZING OF GAIT RESEARCH OBJECTIVE RESEARCH CHALLENGES PURPOSE OF THIS WORK

Freezing of Gait

Irregular gait pattern associated with Parkinson's disease

An episodic inability lasting seconds to generate effective stepping

- Roughly 50% prevalence among PD patients
- Mostly observed during turns, gait initiation, passing narrow spaces, stressful situations, reaching destination
- ▶ Freezing of gait is associated with **falls**
 - ▶ 20-30% of falls lead to mild/severe injuries
 - ▶ 1900 hospital visits in Singapore per year (age>60)
 - Can be expected to grow due to demographic shift



BACKGROUND FEATURE EXTRACTION FEATURE SELECTION CONCLUSION FREEZING OF GAIT **RESEARCH OBJECTIVE** RESEARCH CHALLENGES PURPOSE OF THIS WORK

RESEARCH OBJECTIVE

Objective:

Provide warnings and aid in overcoming FoG by a wearable system

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▶ Provide warnings and aid in overcoming FoG by a wearable system

Detection Systems:

▶ Inertial measurement units (IMUs) worn at lower limbs



Wearable System

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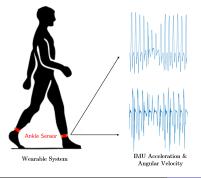


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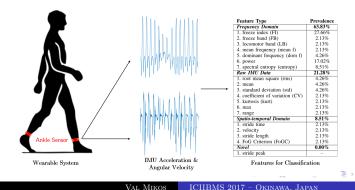


Objective:

▶ Provide warnings and aid in overcoming FoG by a wearable system

Detection Systems:

- Inertial measurement units (IMUs) worn at lower limbs
- ▶ Extract features that correlate well with the occurrence of FoG



Bib.

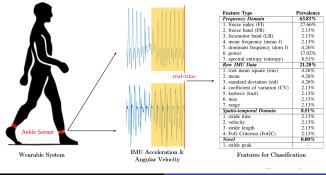


Objective:

▶ Provide warnings and aid in overcoming FoG by a wearable system

Detection Systems:

- Inertial measurement units (IMUs) worn at lower limbs
- Extract features that correlate well with the occurrence of FoG
- Extraction must be in real-time

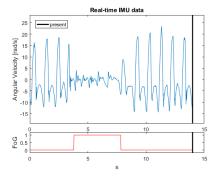


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FREEZING OF GAIT RESEARCH OBJECTIVE **RESEARCH CHALLENGES** PURPOSE OF THIS WORK

Research Challenges – 1. Window Length



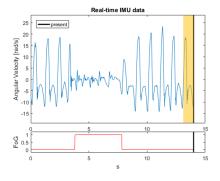
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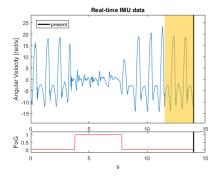
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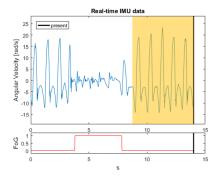
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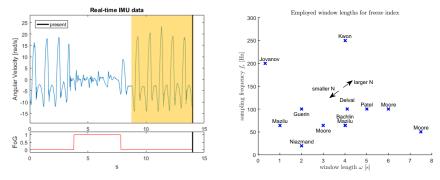


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BACKGROUND FEATURE EXTRACTION FEATURE SELECTION CONCLUSION FREEZING OF GAIT RESEARCH OBJECTIVE **RESEARCH CHALLENGES** PURPOSE OF THIS WORK

Research Challenges – 1. Window Length



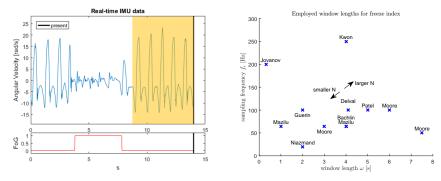
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- Discrepancy in literature

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Research Challenges – 1. Window Length



- What is a good data window length?
- Discrepancy in literature
- Does it matter?

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FREEZING OF GAIT RESEARCH OBJECTIVE **RESEARCH CHALLENGES** PURPOSE OF THIS WORK

Research Challenges – 2. Feature Selection

Feature Type	Prevalence
Frequency Domain	63.83%
1. freeze index (FI)	27.66%
2. freeze band (FB)	2.13%
3. locomotor band (LB)	2.13%
4. mean frequency (mean f)	2.13%
5. dominant frequency (dom f)	4.26%
6. power	17.02%
7. spectral entropy (entropy)	8.51%
Raw IMU Data	21.28%
1. root mean square (rms)	4.26%
2. mean	4.26%
standard deviation (std)	4.26%
4. coefficient of variation (CV)	2.13%
5. kurtosis (kurt)	2.13%
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7. range	2.13%
Spatio-temporal Domain	8.51%
1. stride time	2.13%
2. velocity	2.13%
stride length	2.13%
FoG Criterion (FoGC)	2.13%
Novel	0.00%
1. stride peak	-



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- ▶ What is a good feature subset?
- ▶ No thorough analysis on feature selection for FoG available

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BACKGROUND FEATURE EXTRACTION FEATURE SELECTION CONCLUSION FREEZING OF GAIT RESEARCH OBJECTIVE RESEARCH CHALLENGES **PURPOSE OF THIS WORK**

Purpose of This Work

- 1. Feature Extraction:
 - What are the optimum window lengths?
 - ▶ Does the window length affect classification performance?

2. Feature Selection:

• Given all published IMU features for FOG detection, what are good subset thereof?

How do these compare against previously published feature sets?

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Evaluation Metric Optimal Window Lengths Significance

FEATURE EXTRACTION

Optimal window lengths for feature extraction and their significance.

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Evaluation Metric Optimal Window Lengths Significance

EVALUATION METRIC

▶ How much does knowledge about the extracted feature tell us about the class we are trying to predict?



EVALUATION METRIC

▶ How much does knowledge about the extracted feature tell us about the class we are trying to predict?

Mutual information

$$I(X,Y) = \sum_{x \in X} \sum_{y \in Y} p(x,y) \cdot \log_2\left(\frac{p(x,y)}{p(x) \cdot p(y)}\right)$$

 \blacktriangleright Given feature F extracted with window length ω and the FoG class, find ω which

$$\max_{\omega} I(F(\omega), FoG)$$

- ▶ worst case: $I(F(\omega), FoG) = 0, F(\omega)$ and FoG independent
- best case: $I(F(\omega), FoG) = 1$ bit

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Evaluation Metric Optimal Window Lengths Significance

Optimal Window Lengths – Root Mean Square



Extract feature at various window lengths

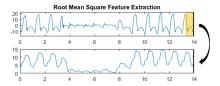
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Evaluation Metric Optimal Window Lengths Significance

Optimal Window Lengths – Root Mean Square



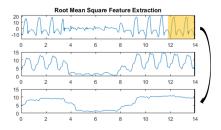
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Evaluation Metric Optimal Window Lengths Significance

Optimal Window Lengths – Root Mean Square



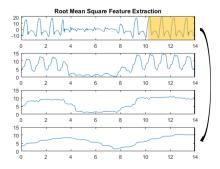
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Evaluation Metric Optimal Window Lengths Significance

Optimal Window Lengths – Root Mean Square



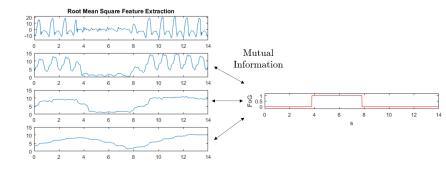
Extract feature at various window lengths

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Evaluation Metric Optimal Window Lengths Significance

Optimal Window Lengths – Root Mean Square



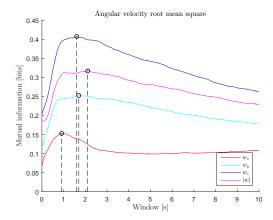
- Extract feature at various window lengths
- Compute mutual information as evaluation metric

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Evaluation Metric Optimal Window Lengths Significance

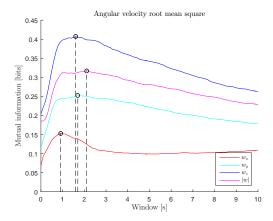
Optimal Window Lengths





Evaluation Metric Optimal Window Lengths Significance

Optimal Window Lengths



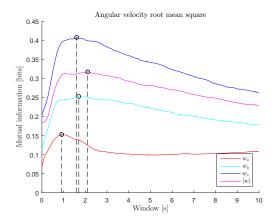
► Angular Velocity RMS $\rightarrow \omega_{opt,x} = 0.9s$ $\rightarrow \omega_{opt,y} = 1.8s$ $\rightarrow \omega_{opt,z} = 1.6s$ $\rightarrow \omega_{opt,||} = 2.1s$

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Evaluation Metric Optimal Window Lengths Significance

Optimal Window Lengths



- Angular Velocity RMS
 - $\rightarrow \omega_{opt,x} = 0.9s$

$$\rightarrow \omega_{opt,y} = 1.8s$$

$$\rightarrow \omega_{opt,z} = 1.6s$$

$$\rightarrow \omega_{opt,||} = 2.1s$$

• Optimal window lengths of 117 features in paper.

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Evaluation Metric Optimal Window Lengths Significance

SIGNIFICANCE – WINDOW LENGTH

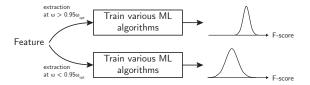
▶ Answering the question: Does it matter?



Evaluation Metric Optimal Window Lengths Significance

SIGNIFICANCE – WINDOW LENGTH

▶ Answering the question: Does it matter?



One-tailed independent t-test

Null hypothesis

$$H_0: f(F_{opt}) \le f(F_{n-opt})$$

Alternative hypothesis

$$H_1: f(F_{opt}) > f(F_{n-opt})$$

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Evaluation Metric Optimal Window Lengths Significance

SIGNIFICANCE

Feature		I(F, FoG)	Window		Performance		Significance		
type	axis	I(r, r 0G)	ω_{opt}	W	$\overline{\mu_{f_1(F_{opt})}}$	$\mu_{f_1(F_{n-opt})}$	$\Delta \mu_{f_1}$	p_{window}	p_{signal}
rms	w_x	0.1539	0.9 s	[0.7, 1.4] s	0.7670	0.7439	0.0231	p < 0.001	
	w_y	0.2553	1.8 s	[0.7, 3.6] s	0.7581	0.7354	0.0227	p < 0.01	p < 0.001
	w_z	0.4078	1.6 s	[0.8, 2.9] s	0.8621	0.7946	0.0675	p < 0.001	p < 0.001
	w	0.3182	2.1 s	[0.8, 3.6] s	0.8409	0.7780	0.0629	p < 0.001	

Alternative Hypothesis (window)

$$H_1: f(F_{opt}) > f(F_{n-opt})$$

- Results of 117 features in paper
- Window length predominantly significant



Maximum Relevance Minimum Redundancy Optimal Feature Subsets Performance Evaluation

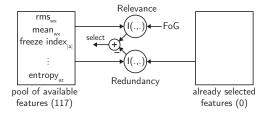
FEATURE SELECTION

Optimal feature subsets for various machine learning algorithms.



MAXIMUM RELEVANCE MINIMUM REDUNDANCY Optimal Feature Subsets Performance Evaluation

MAXIMUM RELEVANCE MINIMUM REDUNDANCY

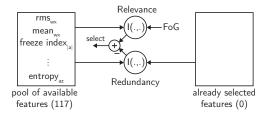


▶ 117 features, $\approx 10^{35}$ feature subset possibilities



MAXIMUM RELEVANCE MINIMUM REDUNDANCY Optimal Feature Subsets Performance Evaluation

MAXIMUM RELEVANCE MINIMUM REDUNDANCY



- ▶ 117 features, $\approx 10^{35}$ feature subset possibilities
- Select the feature F which $\max_{F} \Phi = \alpha \epsilon$

Relevance: $\alpha = I(F, FoG)$ **Redundancy**: $\epsilon = \frac{1}{n} \sum_{i=1}^{n} I(F, F_i)$

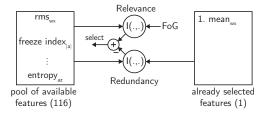
where $F_i, i \in [0, n]$ are already selected features

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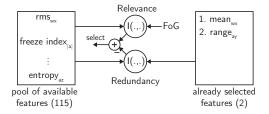
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MAXIMUM RELEVANCE MINIMUM REDUNDANCY Optimal Feature Subsets Performance Evaluation

MAXIMUM RELEVANCE MINIMUM REDUNDANCY



- ▶ 117 features, $\approx 10^{35}$ feature subset possibilities
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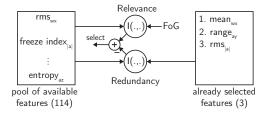
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MAXIMUM RELEVANCE MINIMUM REDUNDANCY



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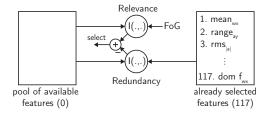
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MAXIMUM RELEVANCE MINIMUM REDUNDANCY Optimal Feature Subsets Performance Evaluation

MAXIMUM RELEVANCE MINIMUM REDUNDANCY



- ▶ 117 features, $\approx 10^{35}$ feature subset possibilities
- Select the feature F which $\max_{F} \Phi = \alpha \epsilon$

Relevance: $\alpha = I(F, FoG)$ **Redundancy**: $\epsilon = \frac{1}{n} \sum_{i=1}^{n} I(F, F_i)$

where $F_i, i \in [0, n]$ are already selected features

 Conventional wrapper method selecting sub-sets on best performing features



MAXIMUM RELEVANCE MINIMUM REDUNDANCY OPTIMAL FEATURE SUBSETS PERFORMANCE EVALUATION

Optimal Feature Subsets

Feature Type	Prevalence
Frequency Domain	63.83%
1. freeze index (FI)	27.66%
2. freeze band (FB)	2.13%
3. locomotor band (LB)	2.13%
4. mean frequency (mean f)	2.13%
5. dominant frequency (dom f)	4.26%
6. power	17.02%
7. spectral entropy (entropy)	8.51%
Raw IMU Data	21.28%
1. root mean square (rms)	4.26%
2. mean	4.26%
3. standard deviation (std)	4.26%
4. coefficient of variation (CV)	2.13%
5. kurtosis (kurt)	2.13%
6. max	2.13%
7. range	2.13%
Spatio-temporal Domain	8.51%
1. stride time	2.13%
2. velocity	2.13%
3. stride length	2.13%
4. FoG Criterion (FoGC)	2.13%
Novel	0.00%
1. stride peak	-

ML algorithm	Feature Subset
SVM	$FI_{ a }, FI_{w_z}, FI_{w_y}, LB_{w_z}, LB_{a_x}, \overline{f_{ w }}, \overline{a_y}, SP$
Neural Nets	$ \begin{array}{l} \operatorname{FI}_{ a }, \ \operatorname{FI}_{w_z}, \ \operatorname{FI}_{w_y}, \ \operatorname{LB}_{w_z}, \ \operatorname{LB}_{a_x}, \ \overline{f_{w_z}}, \ P_{w_z}, \\ S_{a_x}, \ S_{w_y}, \overline{a_y}, \ \operatorname{R}_{w_y}, \ \operatorname{SP} \end{array} $
Log. Regression	$\begin{array}{l} \operatorname{FI}_{ a }, \operatorname{FI}_{w_z}, \operatorname{FI}_{w_y}, \operatorname{LB}_{w_z}, \overline{f_{ w }}, \overline{a_y}, \overline{w_z}, \operatorname{CV}_{a_z}, \\ \operatorname{CV}_{a_y}, \operatorname{V}, \operatorname{SP} \end{array}$
Naïve Bayes	$FI_{ a }, LB_{w_z}$
k-NN	ST, SL, V, SP
DT (C4.5)	FI _{a_x} , LB _{w_z} , LB _{w_y} , $S_{ w }$, S_{w_z} , $\lceil a_y \rceil$, $\lceil w_z \rceil$, K _{w_x} , K _{a_z} , ST, SL, V, SP
Bagging (C4.5)	FI_{a_x} , LB_{w_z} , $\overline{a_y}$, $\overline{w_z}$, R_{w_y}
Boosting (C4.5)	$\frac{\mathrm{FI}_{ a }, \mathrm{FI}_{w_z}, \mathrm{FI}_{a_x}, \mathrm{LB}_{w_z}, \overline{f_{w_z}}, \overline{f_{ w }}, \mathrm{DF}_{a_y}, S_{ w }}{[w_z], \overline{a_y}, \overline{w_y}, \mathrm{K}_{w_x}, \mathrm{CV}_{a_z}, \mathrm{CV}_{w_z}, \mathrm{SL}, \mathrm{V}, \mathrm{SP}}$
Random Forest	FI_{w_z} , DF_{a_y} , S_{w_z} , $\lceil w_z \rceil$, CV_{w_z} , ST, SL, SP

 $\begin{array}{l} \hline Legend: FI_{-}(freeze index), LB_{-}(locomotor band), S_{-}(entropy), \overline{f_{-}(mean frequency)}, \\ DF_{-}(dominant frequency), [_{-}](maximum value), + (mean raw value), K_{-}(kurtosis), \\ CV_{-}(coefficient of variation), R_{-}(range), FoGC (freezing of gait criterion), ST (stride time), SL (stride length), V (velocity), SP (stride peak). \end{array}$



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Log. Regression	$\begin{array}{l} \operatorname{FI}_{ a }, \operatorname{FI}_{w_z}, \operatorname{FI}_{w_y}, \operatorname{LB}_{w_z}, \overline{f_{ w }}, \overline{a_y}, \overline{w_z}, \operatorname{CV}_{a_z}, \\ \operatorname{CV}_{a_y}, \operatorname{V}, \operatorname{SP} \end{array}$
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Bagging (C4.5)	FI_{a_x} , LB_{w_z} , $\overline{a_y}$, $\overline{w_z}$, R_{w_y}
Boosting (C4.5)	$ \begin{array}{c} \operatorname{FI}_{ a }, \operatorname{FI}_{w_z}, \operatorname{FI}_{a_x}, \operatorname{LB}_{w_z}, \overline{f_{w_z}}, \overline{f_{ w }}, \operatorname{DF}_{a_y}, S_{ w }, \\ \lceil w_z \rceil, \overline{a_y}, \overline{w_y}, \operatorname{K}_{w_x}, \operatorname{CV}_{a_z}, \operatorname{CV}_{w_z}, \operatorname{SL}, \operatorname{V}, \operatorname{SP} \end{array} $
Random Forest	FI_{w_z} , DF_{a_y} , S_{w_z} , $\lceil w_z \rceil$, CV_{w_z} , ST, SL, SP



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Spatio-temporal Domain	8.51%
1. stride time	2.13%
2. velocity	2.13%
3. stride length	2.13%
4. FoG Criterion (FoGC)	2.13%
Novel	0.00%
1. stride peak	-

ML algorithm	Feature Subset
SVM	$FI_{ a }, FI_{w_z}, FI_{w_y}, LB_{w_z}, LB_{a_x}, \overline{f_{ w }}, \overline{a_y}, SP$
Neural Nets	$ \begin{array}{c} \operatorname{FI}_{ a }, \ \operatorname{FI}_{w_z}, \ \operatorname{FI}_{w_y}, \ \operatorname{LB}_{w_z}, \ \operatorname{LB}_{a_x}, \ \overline{f_{w_z}}, \ P_{w_z}, \\ S_{a_x}, \ S_{w_y}, \overline{a_y}, \ \operatorname{R}_{w_y}, \ \operatorname{SP} \end{array} $
Log. Regression	$\begin{array}{l} \operatorname{FI}_{ a }, \operatorname{FI}_{w_z}, \operatorname{FI}_{w_y}, \operatorname{LB}_{w_z}, \overline{f_{ w }}, \overline{a_y}, \overline{w_z}, \operatorname{CV}_{a_z}, \\ \operatorname{CV}_{a_y}, \operatorname{V}, \operatorname{SP} \end{array}$
Naïve Bayes	$FI_{ a }, LB_{w_z}$
k-NN	ST, SL, V, SP
DT (C4.5)	FI _{a_x} , LB _{w_z} , LB _{w_y} , $S_{ w }$, S_{w_z} , $\lceil a_y \rceil$, $\lceil w_z \rceil$, K _{w_x} , K _{a_z} , ST, SL, V, SP
Bagging (C4.5)	FI_{a_x} , LB_{w_z} , $\overline{a_y}$, $\overline{w_z}$, R_{w_y}
Boosting (C4.5)	$ \begin{array}{c} \operatorname{FI}_{ a }, \operatorname{FI}_{w_z}, \operatorname{FI}_{a_x}, \operatorname{LB}_{w_z}, \overline{f_{w_z}}, \overline{f_{ w }}, \operatorname{DF}_{a_y}, S_{ w }, \\ \lceil w_z \rceil, \overline{a_y}, \overline{w_y}, \operatorname{K}_{w_x}, \operatorname{CV}_{a_z}, \operatorname{CV}_{w_z}, \operatorname{SL}, \operatorname{V}, \operatorname{SP} \end{array} $
Random Forest	FI_{w_z} , DF_{a_y} , S_{w_z} , $\lceil w_z \rceil$, CV_{w_z} , ST, SL, SP



MAXIMUM RELEVANCE MINIMUM REDUNDANCY OPTIMAL FEATURE SUBSETS PERFORMANCE EVALUATION

Optimal Feature Subsets

Feature Type	Prevalence
Frequency Domain	63.83%
1. freeze index (FI)	27.66%
2. freeze band (FB)	2.13%
3. locomotor band (LB)	2.13%
4. mean frequency (mean f)	2.13%
5. dominant frequency (dom f)	4.26%
6. power	17.02%
7. spectral entropy (entropy)	8.51%
Raw IMU Data	21.28%
1. root mean square (rms)	4.26%
2. mean	4.26%
3. standard deviation (std)	4.26%
4. coefficient of variation (CV)	2.13%
5. kurtosis (kurt)	2.13%
6. max	2.13%
7. range	2.13%
Spatio-temporal Domain	8.51%
1. stride time	2.13%
2. velocity	2.13%
3. stride length	2.13%
4. FoG Criterion (FoGC)	2.13%
Novel	0.00%
1. stride peak	-

ML algorithm	Feature Subset
SVM	$FI_{ a }, FI_{w_z}, FI_{w_y}, LB_{w_z}, LB_{a_x}, \overline{f_{ w }}, \overline{a_y}, SP$
Neural Nets	$ \begin{array}{c} \operatorname{FI}_{ a }, \ \operatorname{FI}_{w_z}, \ \operatorname{FI}_{w_y}, \ \operatorname{LB}_{w_z}, \ \operatorname{LB}_{a_x}, \ \overline{f_{w_z}}, \ P_{w_z}, \\ S_{a_x}, \ S_{w_y}, \overline{a_y}, \ \operatorname{R}_{w_y}, \ \operatorname{SP} \end{array} $
Log. Regression	$\begin{array}{l} \operatorname{FI}_{ a }, \operatorname{FI}_{w_z}, \operatorname{FI}_{w_y}, \operatorname{LB}_{w_z}, \overline{f_{ w }}, \overline{a_y}, \overline{w_z}, \operatorname{CV}_{a_z}, \\ \operatorname{CV}_{a_y}, \operatorname{V}, \operatorname{SP} \end{array}$
Naïve Bayes	$FI_{ a }, LB_{w_z}$
k-NN	ST, SL, V, SP
DT (C4.5)	FI _{a_x} , LB _{w_z} , LB _{w_y} , $S_{ w }$, S_{w_z} , $\lceil a_y \rceil$, $\lceil w_z \rceil$, K _{w_x} , K _{a_z} , ST, SL, V, SP
Bagging (C4.5)	FI_{a_x} , LB_{w_z} , $\overline{a_y}$, $\overline{w_z}$, R_{w_y}
Boosting (C4.5)	$ \begin{array}{c} \operatorname{FI}_{ a }, \operatorname{FI}_{w_z}, \operatorname{FI}_{a_x}, \operatorname{LB}_{w_z}, \overline{f_{w_z}}, \overline{f_{ w }}, \operatorname{DF}_{a_y}, S_{ w }, \\ \lceil w_z \rceil, \overline{a_y}, \overline{w_y}, \operatorname{K}_{w_x}, \operatorname{CV}_{a_z}, \operatorname{CV}_{w_z}, \operatorname{SL}, \operatorname{V}, \operatorname{SP} \end{array} $
Random Forest	FI_{w_z} , DF_{a_y} , S_{w_z} , $\lceil w_z \rceil$, CV_{w_z} , ST, SL, SP



MAXIMUM RELEVANCE MINIMUM REDUNDANCY OPTIMAL FEATURE SUBSETS PERFORMANCE EVALUATION

Optimal Feature Subsets

Feature Type	Prevalence
Frequency Domain	63.83%
1. freeze index (FI)	27.66%
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Spatio-temporal Domain	8.51%
1. stride time	2.13%
2. velocity	2.13%
3. stride length	2.13%
4. FoG Criterion (FoGC)	2.13%
Novel	0.00%
1. stride peak	-

ML algorithm	Feature Subset
SVM	$FI_{ a }, FI_{w_z}, FI_{w_y}, LB_{w_z}, LB_{a_x}, \overline{f_{ w }}, \overline{a_y}, SP$
Neural Nets	$ \begin{array}{c} \operatorname{FI}_{ a }, \ \operatorname{FI}_{w_z}, \ \operatorname{FI}_{w_y}, \ \operatorname{LB}_{w_z}, \ \operatorname{LB}_{a_x}, \ \overline{f_{w_z}}, \ P_{w_z}, \\ S_{a_x}, \ S_{w_y}, \overline{a_y}, \ \operatorname{R}_{w_y}, \ \operatorname{SP} \end{array} $
Log. Regression	$\begin{array}{l} \operatorname{FI}_{ a }, \operatorname{FI}_{w_z}, \operatorname{FI}_{w_y}, \operatorname{LB}_{w_z}, \overline{f_{ w }}, \overline{a_y}, \overline{w_z}, \operatorname{CV}_{a_z}, \\ \operatorname{CV}_{a_y}, \operatorname{V}, \operatorname{SP} \end{array}$
Naïve Bayes	$FI_{ a }$, LB_{w_z}
k-NN	ST, SL, V, SP
DT (C4.5)	$ \begin{array}{c} \operatorname{FI}_{a_x}, \operatorname{LB}_{w_z}, \operatorname{LB}_{w_y}, S_{ w }, S_{w_z}, [a_y], [w_z], \\ \operatorname{K}_{w_x}, \operatorname{K}_{a_z}, \operatorname{ST}, \operatorname{SL}, \operatorname{V}, \operatorname{SP} \end{array} $
Bagging (C4.5)	FI_{a_x} , LB_{w_z} , $\overline{a_y}$, $\overline{w_z}$, R_{w_y}
Boosting (C4.5)	$ \begin{array}{c} \operatorname{FI}_{ a }, \operatorname{FI}_{w_z}, \operatorname{FI}_{a_x}, \operatorname{LB}_{w_z}, \overline{f_{w_z}}, \overline{f_{ w }}, \operatorname{DF}_{a_y}, S_{ w }, \\ \lceil w_z \rceil, \overline{a_y}, \overline{w_y}, \operatorname{K}_{w_x}, \operatorname{CV}_{a_z}, \operatorname{CV}_{w_z}, \operatorname{SL}, \operatorname{V}, \operatorname{SP} \end{array} $
Random Forest	FI_{w_z} , DF_{a_y} , S_{w_z} , $\lceil w_z \rceil$, CV_{w_z} , ST, SL, SP

 $\begin{array}{l} \hline Legend: FI_{-}(freeze index), LB_{-}(locomotor band), S_{-}(entropy), \overline{f_{-}(mean frequency)}, \\ DF_{-}(dominant frequency), [_{-}](maximum value), + (mean raw value), K_{-}(kurtosis), \\ CV_{-}(coefficient of variation), R_{-}(range), FoGC (freezing of gait criterion), ST (stride time), SL (stride length), V (velocity), SP (stride peak). \end{array}$



MAXIMUM RELEVANCE MINIMUM REDUNDANCY OPTIMAL FEATURE SUBSETS PERFORMANCE EVALUATION

Optimal Feature Subsets

Feature Type	Prevalence
Frequency Domain	63.83%
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1. root mean square (rms)	4.26%
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5. kurtosis (kurt)	2.13%
6. max	2.13%
7. range	2.13%
Spatio-temporal Domain	8.51%
1. stride time	2.13%
2. velocity	2.13%
3. stride length	2.13%
4. FoG Criterion (FoGC)	2.13%
Novel	0.00%
1. stride peak	-

ML algorithm	Feature Subset
SVM	$FI_{ a }, FI_{w_z}, FI_{w_y}, LB_{w_z}, LB_{a_x}, \overline{f_{ w }}, \overline{a_y}, SP$
Neural Nets	$ \begin{array}{l} \operatorname{FI}_{ a }, \ \operatorname{FI}_{w_z}, \ \operatorname{FI}_{w_y}, \ \operatorname{LB}_{w_z}, \ \operatorname{LB}_{a_x}, \ \overline{f_{w_z}}, \ P_{w_z}, \\ S_{a_x}, \ S_{w_y}, \overline{a_y}, \ \operatorname{R}_{w_y}, \ \operatorname{SP} \end{array} $
Log. Regression	$\begin{array}{l} \operatorname{FI}_{ a }, \operatorname{FI}_{w_z}, \operatorname{FI}_{w_y}, \operatorname{LB}_{w_z}, \overline{f_{ w }}, \overline{a_y}, \overline{w_z}, \operatorname{CV}_{a_z}, \\ \operatorname{CV}_{a_y}, \operatorname{V}, \operatorname{SP} \end{array}$
Naïve Bayes	$FI_{ a }, LB_{w_z}$
k-NN	ST, SL, V, SP
DT (C4.5)	FI _{a_x} , LB _{w_z} , LB _{w_y} , $S_{ w }$, S_{w_z} , $\lceil a_y \rceil$, $\lceil w_z \rceil$, K _{w_x} , K _{a_z} , ST, SL, V, SP
Bagging (C4.5)	FI_{a_x} , LB_{w_z} , $\overline{a_y}$, $\overline{w_z}$, R_{w_y}
Boosting (C4.5)	$\frac{\mathrm{FI}_{ a }, \mathrm{FI}_{w_z}, \mathrm{FI}_{a_x}, \mathrm{LB}_{w_z}, \overline{f_{w_z}}, \overline{f_{ w }}, \mathrm{DF}_{a_y}, S_{ w }}{[w_z], \overline{a_y}, \overline{w_y}, \mathrm{K}_{w_x}, \mathrm{CV}_{a_z}, \mathrm{CV}_{w_z}, \mathrm{SL}, \mathrm{V}, \mathrm{SP}}$
Random Forest	FI_{w_z} , DF_{a_y} , S_{w_z} , $\lceil w_z \rceil$, CV_{w_z} , ST, SL, SP

 $\begin{array}{l} \hline Legend: FI_{-}(freeze index), LB_{-}(locomotor band), S_{-}(entropy), \overline{f_{-}(mean frequency)}, \\ DF_{-}(dominant frequency), [_{-}](maximum value), + (mean raw value), K_{-}(kurtosis), \\ CV_{-}(coefficient of variation), R_{-}(range), FoGC (freezing of gait criterion), ST (stride time), SL (stride length), V (velocity), SP (stride peak). \end{array}$



MAXIMUM RELEVANCE MINIMUM REDUNDANCY OPTIMAL FEATURE SUBSETS PERFORMANCE EVALUATION

Optimal Feature Subsets

1. freeze index (FI) 27.66% 2. freeze band (FB) 2.13% 3. locomotor band (LB) 2.13% 4. mean frequency (mean f) 2.13% 5. dominant frequency (mean f) 2.13% 6. power 17.02% 7. spectral entropy (entropy) 8.51% 8. standard deviation (std) 4.26% 2. mean 4.26% 3. standard deviation (std) 4.26% 5. kurtosis (kurt) 2.13% 5. kurtosis (kurt) 2.13% 7. range 2.13% 8.519% 1. stride time 2. velocity 2.13% 3. stride length 2.13% 4. FOG Criterion (FoGC) 2.13%	Feature Type	Prevalence
2. freeze band (FB) 2.13% 3. locomotor band (LB) 2.13% 4. mean frequency (mean f) 2.13% 5. dominant frequency (dom f) 4.26% 6. power 17.02% 7. spectral entropy (entropy) 8.51% 1. root mean square (rms) 4.26% 2. mean 4.26% 3. standard deviation (std) 4.26% 6. max 2.13% 7. range 2.13% 7. range 2.13% 1. stride time 2.13% 2. velocity 2.13% 3. stride length 2.13% 4. FloG Criterion (FoGC) 2.13%	Frequency Domain	63.83%
3. locomotor band (LB) 2.13% 4. mean frequency (mean f) 2.13% 5. dominant frequency (dom f) 2.66% 7. spectral entropy (entropy) 8.51% <i>Raw IMU Data</i> 21.28% 1. root mean square (rms) 4.26% 2. mean 4.26% 3. standard deviation (std) 4.26% 4. coefficient of variation (CV) 2.13% 5. kurtosis (kurt) 2.13% 6. max 2.13% 7. range 2.13% 2. velocity 2.13% 3. stride length 2.13% 4. FoG Criterion (FoGC) 2.13%	1. freeze index (FI)	27.66%
4. mean frequency (mean f) 2.13% 5. dominant frequency (dom f) 4.26% 6. power 17.02% 7. spectral entropy (entropy) 8.51% Raw IMU Data 21.28% 1. root mean square (rms) 4.26% 3. standard deviation (std) 4.26% 4. coefficient of variation (CV) 2.13% 5. kurtosis (kurt) 2.13% 5. kurtosis (kurt) 2.13% 5. kurtosis (kurt) 2.13% 5. kurtosis (kurt) 2.13% 2. velocity 2.13% 3. stride length 2.13% 4. FOG Criterion (FoGC) 2.13%	2. freeze band (FB)	2.13%
5. dominant frequency (dom f) 4.26% 6. power 17.02% 7. spectral entropy (entropy) 8.51% Raw IMU Data 21.28% 1. root mean square (rms) 4.26% 2. mean 4.26% 3. standard deviation (std) 4.26% 4. coefficient of variation (CV) 2.13% 5. kurtosis (kurt) 2.13% 6. max 2.13% 7. range 2.13% 9, stride time 2.13% 2. velocity 2.13% 3. stride length 2.13% 4. FoG Criterion (FoGC) 2.13% 4. FoG Criterion (FoGC) 2.13%	3. locomotor band (LB)	2.13%
6. power 17.02% 7. spectral entropy (entropy) 8.51% <i>Raw IMU Data</i> 21.28% 1. root mean square (rms) 4.26% 2. mean 4.26% 3. standard deviation (std) 4.26% 4. coefficient of variation (CV) 2.13% 5. kurtosis (kurt) 2.13% 6. max 2.13% 7. range 2.13% Spatio-temporal Domain 8.51% 1. stride time 2.13% 2. velocity 2.13% 3. stride length 2.13% 4. FOG Criterion (FoGC) 2.13% Novel 0.00%	4. mean frequency (mean f)	2.13%
7. spectral entropy (entropy) 8.51% Raw IMU Data 21.28% 1. root mean square (rms) 4.26% 2. mean 4.26% 3. standard deviation (std) 4.26% 6. max 2.13% 7. range 2.13% 7. range 2.13% 9. standard deviation (std) 2.65% 8. standard deviation (std) 2.13% 7. range 2.13% 9. staride time 2.13% 1. stride time 2.13% 2. velocity 2.13% 3. stride length 2.13% 4. FoG Criterion (FoGC) 2.13% Movel 0.00%	5. dominant frequency (dom f)	4.26%
Raw IMU Data 21.28% 1. root mean square (rms) 4.26% 2. mean 4.26% 3. standard deviation (std) 4.26% 4. coefficient of variation (CV) 2.13% 5. kurtosis (kurt) 2.13% 6. max 2.13% 7. range 2.13% Spatio-temporal Domain 8.51% 1. stride time 2.13% 2. velocity 2.13% 3. stride length 2.13% 4. FoG Criterion (FoGC) 2.13% Novel 0.00%	6. power	17.02%
1. root mean square (rms) 4.26% 2. mean 4.26% 3. standard deviation (std) 4.26% 4. coefficient of variation (CV) 2.13% 5. kurtosis (kurt) 2.13% 5. kurtosis (kurt) 2.13% 5. kurtosis (kurt) 2.13% 5. kurtosis (kurt) 8.51% 1. stride time 2.13% 5. velocity 2.13% 2. velocity 2.13% 3. stride length 2.13% 4. FoG Criterion (FoGC) 2.13% Novel 0.00%	7. spectral entropy (entropy)	8.51%
2. mean 4.26% 3. standard deviation (std) 4.26% 4. coefficient of variation (CV) 2.13% 5. kurtosis (kurt) 2.13% 6. max 2.13% 7. range 2.13% 2. raide time 2.13% 2. velocity 2.13% 3. stride length 2.13% 4. FoG Criterion (FoGC) 2.13% Novel 0.00%	Raw IMU Data	21.28%
3. standard deviation (std) 4.26% 4. coefficient of variation (CV) 2.13% 5. kurtosis (kurt) 2.13% 6. max 2.13% 7. range 2.13% Spatio-temporal Domain 8.51% 1. stride time 2.13% 2. velocity 2.13% 3. stride length 2.13% 4. FOG Criterion (FoGC) 2.13% Novel 0.00%	1. root mean square (rms)	4.26%
4. coefficient of variation (CV) 2.13% 5. kurtosis (kurt) 2.13% 6. max 2.13% 7. range 2.13% 8. Staff 8.51% 1. stride time 2.13% 2. velocity 2.13% 3. stride length 2.13% 4. FoG Criterion (FoGC) 2.13% Movel 0.00%	2. mean	4.26%
5. kurtosis (kurt) 2.13% 6. max 2.13% 7. range 2.13% Spatio-temporal Domain 8.51% 1. stride time 2.13% 2. velocity 2.13% 3. stride length 2.13% 4. FoG Criterion (FoGC) 2.13% Novel 0.00%	3. standard deviation (std)	4.26%
6. max 2.13% 7. range 2.13% Spatio-temporal Domain 8.51% 1. stride time 2.13% 2. velocity 2.13% 3. stride length 2.13% 4. FoG Criterion (FoGC) 2.13% Novel 0.00%	4. coefficient of variation (CV)	2.13%
7. range 2.13% Spatio-temporal Domain 8.51% 1. stride time 2.13% 2. velocity 2.13% 3. stride length 2.13% 4. FoG Criterion (FoGC) 2.13% Novel 0.00%	5. kurtosis (kurt)	2.13%
Spatio-temporal Domain 8.51% 1. stride time 2.13% 2. velocity 2.13% 3. stride length 2.13% 4. FoG Criterion (FoGC) 2.13% Novel 0.00%	6. max	2.13%
1. stride time 2.13% 2. velocity 2.13% 3. stride length 2.13% 4. FoG Criterion (FoGC) 2.13% Novel 0.00%	7. range	2.13%
2. velocity 2.13% 3. stride length 2.13% 4. FoG Criterion (FoGC) 2.13% Novel 0.00%	Spatio-temporal Domain	
3. stride length 2.13% 4. FoG Criterion (FoGC) 2.13% Novel 0.00%	1. stride time	2.13%
4. FoG Criterion (FoGC) 2.13% Novel 0.00%	2. velocity	2.13%
Novel 0.00%		2.13%
	4. FoG Criterion (FoGC)	2.13%
1. stride peak -	Novel	0.00%
	1. stride peak	-

ML algorithm	Feature Subset
SVM	$FI_{ a }, FI_{w_z}, FI_{w_y}, LB_{w_z}, LB_{a_x}, \overline{f_{ w }}, \overline{a_y}, SP$
Neural Nets	$ \begin{array}{c} FI_{ a }, \ FI_{w_z}, \ FI_{w_y}, \ LB_{w_z}, \ LB_{a_x}, \ \overline{f_{w_z}}, \ P_{w_z}, \\ S_{a_x}, \ S_{w_y}, \ \overline{a_y}, \ R_{w_y}, \ SP \end{array} $
Log. Regression	$\begin{array}{c} \operatorname{FI}_{ a }, \operatorname{FI}_{w_z}, \operatorname{FI}_{w_y}, \operatorname{LB}_{w_z}, \overline{f_{ w }}, \overline{a_y}, \overline{w_z}, \operatorname{CV}_{a_z}, \\ \operatorname{CV}_{a_y}, \operatorname{V}, \operatorname{SP} \end{array}$
Naïve Bayes	$FI_{ a }, LB_{w_z}$
k-NN	ST, SL, V, SP
DT (C4.5)	FI _{a_x} , LB _{w_z} , LB _{w_y} , $S_{ w }$, S_{w_z} , $\lceil a_y \rceil$, $\lceil w_z \rceil$, K _{w_x} , K _{a_z} , ST, SL, V, SP
Bagging (C4.5)	$FI_{a_x}, LB_{w_z}, \overline{a_y}, \overline{w_z}, R_{w_y}$
Boosting (C4.5)	$ \begin{array}{c} \operatorname{FI}_{ a }, \operatorname{FI}_{w_z}, \operatorname{FI}_{a_x}, \operatorname{LB}_{w_z}, \overline{f_{w_z}}, \overline{f_{ w }}, \operatorname{DF}_{a_y}, S_{ w }, \\ \lceil w_z \rceil, \overline{a_y}, \overline{w_y}, \operatorname{K}_{w_x}, \operatorname{CV}_{a_z}, \operatorname{CV}_{w_z}, \operatorname{SL}, \operatorname{V}, \operatorname{SP} \end{array} $
Random Forest	FI_{w_z} , DF_{a_y} , S_{w_z} , $\lceil w_z \rceil$, CV_{w_z} , ST, SL, SP

 $\begin{array}{l} \hline Legend: FI_{-}(freeze index), LB_{-}(locomotor band), S_{-}(entropy), \overline{f_{-}(mean frequency)}, \\ DF_{-}(dominant frequency), [_{-}](maximum value), + (mean raw value), K_{-}(kurtosis), \\ CV_{-}(coefficient of variation), R_{-}(range), FoGC (freezing of gait criterion), ST (stride time), SL (stride length), V (velocity), SP (stride peak). \end{array}$



MAXIMUM RELEVANCE MINIMUM REDUNDANCY OPTIMAL FEATURE SUBSETS PERFORMANCE EVALUATION

Optimal Feature Subsets

Feature Type	Prevalence
Frequency Domain	63.83%
1. freeze index (FI)	27.66%
2. freeze band (FB)	2.13%
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3. stride length	2.13%
4. FoG Criterion (FoGC)	2.13%
Novel	0.00%
1. stride peak	-

ML algorithm	Feature Subset
SVM	$FI_{ a }, FI_{w_z}, FI_{w_y}, LB_{w_z}, LB_{a_x}, \overline{f_{ w }}, \overline{a_y}, SP$
Neural Nets	$ \begin{array}{c} FI_{ a }, \ FI_{w_z}, \ FI_{w_y}, \ LB_{w_z}, \ LB_{a_x}, \ \overline{f_{w_z}}, \ P_{w_z}, \\ S_{a_x}, \ S_{w_y}, \ \overline{a_y}, \ R_{w_y}, \ SP \end{array} $
Log. Regression	$\begin{array}{c} \operatorname{FI}_{ a }, \operatorname{FI}_{w_z}, \operatorname{FI}_{w_y}, \operatorname{LB}_{w_z}, \overline{f_{ w }}, \overline{a_y}, \overline{w_z}, \operatorname{CV}_{a_z}, \\ \operatorname{CV}_{a_y}, \operatorname{V}, \operatorname{SP} \end{array}$
Naïve Bayes	$FI_{ a }$, LB_{w_z}
k-NN	ST, SL, V, SP
DT (C4.5)	FI _{a_x} , LB _{w_z} , LB _{w_y} , $S_{ w }$, S_{w_z} , $\lceil a_y \rceil$, $\lceil w_z \rceil$, K _{w_x} , K _{a_z} , ST, SL, V, SP
Bagging (C4.5)	$FI_{a_x}, LB_{w_z}, \overline{a_y}, \overline{w_z}, R_{w_y}$
Boosting (C4.5)	$ \begin{array}{c} \operatorname{FI}_{ a }, \operatorname{FI}_{w_z}, \operatorname{FI}_{a_x}, \operatorname{LB}_{w_z}, \overline{f_{w_z}}, \overline{f_{ w }}, \operatorname{DF}_{a_y}, S_{ w }, \\ \lceil w_z \rceil, \overline{a_y}, \overline{w_y}, \operatorname{K}_{w_x}, \operatorname{CV}_{a_z}, \operatorname{CV}_{w_z}, \operatorname{SL}, \operatorname{V}, \operatorname{SP} \end{array} $
Random Forest	FI_{w_z} , DF_{a_y} , S_{w_z} , $\lceil w_z \rceil$, CV_{w_z} , ST, SL, SP

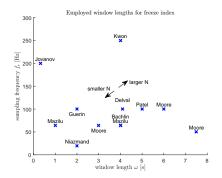
Legend: FI. (freeze index), LB. (locomotor band), S. (entropy), \overline{f} . (mean frequency), DF. (dominant frequency), [.-] (maximum value), τ (mean raw value), K. (kurtosis), CV. (coefficient of variation), R. (range), FoGC (freezing of gait criterion), ST (stride time), SL (stride length), V (velocity), SP (stride peak).



MAXIMUM RELEVANCE MINIMUM REDUNDANCY Optimal Feature Subsets Performance Evaluation

PERFORMANCE EVALUATION

Feature sets	Our	Bächlin	Mazilu	Tripoliti	Coste
Feature Count	2-17	2	7	3	1
$\omega \in \mathcal{W}, N \in \mathcal{N}$	100%	50%	14.2%	0%	-
Machine learning	algoritl	ims			
SVM					
Neural Nets					
Log. Regression					
Naive Bayes					
k-NN					
DT (C4.5)					
Bagging (C4.5)					
Boosting (C4.5)					
Random Forest					
Average					



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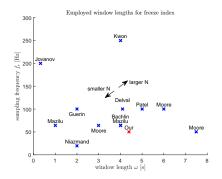
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MAXIMUM RELEVANCE MINIMUM REDUNDANCY Optimal Feature Subsets Performance Evaluation

PERFORMANCE EVALUATION

Feature sets	Our	Bächlin	Mazilu	Tripoliti	Coste
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$\omega \in \mathcal{W}, N \in \mathcal{N}$	100%	50%	14.2%	0%	-
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SVM					
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Bagging (C4.5)					
Boosting (C4.5)					
Random Forest					
Average					



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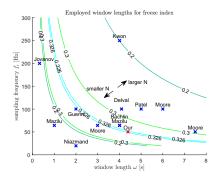
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MAXIMUM RELEVANCE MINIMUM REDUNDANCY Optimal Feature Subsets Performance Evaluation

PERFORMANCE EVALUATION

Feature sets	Our	Bächlin	Mazilu	Tripoliti	Coste
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Machine learning	algoriti	hms			
SVM					
Neural Nets					
Log. Regression					
Naive Bayes					
k-NN					
DT (C4.5)					
Bagging (C4.5)					
Boosting (C4.5)					
Random Forest					
Average					



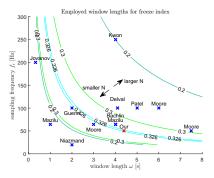
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MAXIMUM RELEVANCE MINIMUM REDUNDANCY Optimal Feature Subsets **Performance Evaluation**

PERFORMANCE EVALUATION

Feature sets	Our	Bächlin	Mazilu	Tripoliti	Coste
Feature Count	2-17	2	7	3	1
$\omega \in \mathcal{W}, N \in \mathcal{N}$	100%	50%	14.2%	0%	-
Machine learning	algoriti	hms			
SVM	0.880	0.860	0.862	0.800	0.782
Neural Nets	0.872	0.859	0.852	0.747	0.745
Log. Regression	0.880	0.857	0.861	0.811	0.774
Naive Bayes	0.875	0.867	0.795	0.782	0.785
k-NN	0.801	0.797	0.800	0.678	0.709
DT (C4.5)	0.845	0.838	0.809	0.770	0.700
Bagging (C4.5)	0.852	0.842	0.824	0.751	0.702
Boosting (C4.5)	0.871	0.821	0.834	0.727	0.700
Random Forest	0.878	0.824	0.832	0.738	0.709
Average	0.861	0.841	0.830	0.756	0.734



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▶ Feature selection creates favorable subsets that outperform the arbitrary assembled feature sets in literature.



CONCLUSION

Purpose revisited.

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- 1. Feature Extraction:
 - ▶ What are the optimum window lengths?
 - ▶ Does the window length affect classification performance?

2. Feature Selection:

- Given all published IMU features for FOG detection, what are good subset thereof?
- How do these compare against previously published feature sets?

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- 1. Feature Extraction:
 - What are the optimum window lengths?
 Identified the optimal window length for 117 features.
 - Does the window length affect classification performance?

2. Feature Selection:

- Given all published IMU features for FOG detection, what are good subset thereof?
- How do these compare against previously published feature sets?

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- 1. Feature Extraction:
 - What are the optimum window lengths?
 Identified the optimal window length for 117 features.
 - Does the window length affect classification performance? It significantly affects classification performance for the majority of features.

2. Feature Selection:

- Given all published IMU features for FOG detection, what are good subset thereof?
- How do these compare against previously published feature sets?

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The feature subsets have been found for 9 machine learning algorithms.

▶ How do these compare against previously published feature sets?

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- 1. Feature Extraction:
 - What are the optimum window lengths?
 Identified the optimal window length for 117 features.
 - Does the window length affect classification performance? It significantly affects classification performance for the majority of features.

2. Feature Selection:

• Given all published IMU features for FOG detection, what are good subset thereof?

The feature subsets have been found for 9 machine learning algorithms.

 How do these compare against previously published feature sets? Extraction at optimal window lengths and feature selection creates favorable classification performance.

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THANK YOU!

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- L. Tan, N. Venketasubramanian, C. Hong, S. Sahadevan, J. Chin, E. Krishnamoorthy, A. Tan, and S. Saw, *Prevalence of parkinson disease in singapore chinese vs malays vs indians*, Neurology, vol. 62, no. 11, pp. 1999-2004, 2004.
- [2] Department of Statistics, Republic of Singapore, *Population trends 2016*, http://www.singstat.gov.sg/docs/, September 2016. accessed: 31.10.2016.
- [3] Committe on Ageing Issues, Republic of Singapore, *Report on the ageing population.* https://app.msf.gov.sg, February 2006. accessed: 31.10.2016.
- [4] Y. J. Zhao, L. C. S. Tan, S. C. Li, W. L. Au, S. H. Seah, P. N. Lau, N. Luo, and H. L. Wee, *Economic burden of parkinsons disease in singapore*, European Journal of Neurology, vol. 18, no. 3, pp. 519-526, 2011.
- [5] Y. J. Zhao, L. C. S. Tan, W. L. Au, D. M. K. Heng, I. A. L. Soh, S. C. Li, N. Luo, and H. L. Wee, *Estimating the lifetime economic burden of parkinsons disease in singapore*, European Journal of Neurology, vol. 20, no. 2, pp. 368-374, 2013.

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- [6] N. Giladi and A. Nieuwboer, Understanding and treating freezing of gait in parkinsonism, proposed working definition, and setting the stage, Movement Disorders, vol. 23, no. S2, pp. S423-S425, 2008.
- [7] M. Macht, Y. Kaussner, J. C. Mller, K. Stiasny-Kolster, K. M. Eggert, H.-P. Krger, and H. Ellgring, *Predictors of freezing in parkinsons disease: a survey of 6,620 patients*, Movement Disorders, vol. 22, no. 7, pp. 953-956, 2007.
- [8] J. D. Schaafsma, Y. Balash, T. Gurevich, A. L. Bartels, J. M. Hausdorff, and N. Giladi, *Characterization of freezing of gait subtypes and the response of each to levodopa in parkinsons disease*, European Journal of Neurology, vol. 10, no. 4, pp. 391-398, 2003.
- [9] J.Spildooren, S.Vercruysse, K.Desloovere, W.Vandenberghe, E.Kerckhofs, and A.Nieuwboer, Freezing of gait in parkinsons disease: the impact of dual-tasking and turning, Movement Disorders, vol. 25, no. 15, pp. 2563-2570, 2010.
- [10] B. R. Bloem, J. M. Hausdorff, J. E. Visser, and N. Giladi, Falls and freezing of gait in parkinsons disease: a review of two interconnected, episodic phenomena, Movement Disorders, vol. 19, no. 8, pp. 871-884, 2004



- [11] M. D. Latt, S. R. Lord, J. G. Morris, and V. S. Fung, *Clinical and physiological assessments for elucidating falls risk in parkinsons disease*, Movement Disorders, vol.24, no.9, pp.1280-1289, 2009.
- [12] WHO Ageing and LC Unit, WHO global report on falls prevention in older age. World Health Organization, 2008.
- [13] G. MM., Medical management of parkinson's disease, Pharmacy and Therapeutics, vol. 33, no. 10, pp. 590-606, 2008.
- [14] A.Barbeau, L-dopa therapy in parkinson's disease: a critical review of nine years' experience, Canadian Medical Association Journal, vol. 101, no. 13, p. 59, 1969.
- [15] T. Hashimoto, Speculation on the responsible sites and pathophysiology of freezing of gait, Parkinsonism & Related Disorders, vol. 12, pp. S55-S62, 2006.
- [16] J. E. Ahlskog and M. D. Muenter, Frequency of levodopa-related dyskinesias and motor fluctuations as estimated from the cumulative literature, Movement disorders, vol. 16, no. 3, pp. 448-458, 2001.

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- [17] M. S. Okun and P. R. Zeilman, Parkinsons disease: Guide to deep brain stimulation therapy, second edition (2014). http://www.parkinson.org/sites/default /files/Guide_to_DBS_Stimulation_Therapy.pdf. National Parkinson Foundation, accessed: 08.09.2016.
- [18] F. M. Weaver, K. Follett, M. Stern, K. Hur, C. Harris, W. J. Marks, J. Rothlind, O. Sagher, D. Reda, C. S. Moy, et al., *Bilateral deep brain stimulation vs best* medical therapy for patients with advanced parkinson disease: a randomized controlled trial, Journal of the American Medical Association, vol. 301, no. 1, pp. 63-73, 2009.
- [19] J. Lazarus, Medications for motor symptoms and surgical treatment options. http://www.parkinson.org/understanding-parkinsons/treatment. National Parkinson Foundation, accessed: 08.09.2016.
- [20] M. Rodriguez-Oroz, J. Obeso, A. Lang, J.-L. Houeto, P. Pollak, S. Rehncrona, J. Kulisevsky, A. Albanese, J. Volkmann, M. Hariz, et al., *Bilateral deep brain* stimulation in parkinsons disease: a multicentre study with 4 years follow-up, Brain, vol. 128, no. 10, pp. 2240-2249, 2005.



- [21] A. Delval, C. Moreau, S. Bleuse, C. Tard, G. Ryckewaert, D. Devos, and L. Defebvre, Auditory cueing of gait initiation in parkinsons disease patients with freezing of gait, Clinical Neurophysiology, vol. 125, no. 8, pp. 1675-1681, 2014.
- [22] P. J. McCandless, B. J. Evans, J. Janssen, J. Selfe, A. Churchill, and J. Richards, Effect of three cueing devices for people with Parkinsons disease with gait initiation difficulties, Gait & Posture, vol. 44, pp. 711, 2016.
- [23] A. Nieuwboer, G. Kwakkel, L. Rochester, D. Jones, E. van Wegen, A. M. Willems, F. Chavret, V. Hetherington, K. Baker, and I. Lim, *Cueing training in the home improves gait-related mobility in parkinsons disease: the rescue trial*, Journal of Neurology, Neurosurgery & Psychiatry, vol. 78, no. 2, pp. 134-140, 2007.
- [24] J. H. Bergmann, V. Chandaria, and A. McGregor, Wearable and implantable sensors: the patients perspective, Sensors, vol. 12, no. 12, pp. 16695-16709, 2012.

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